# Home Assignment ( Set - 01) <br> Numerical Methods <br> Paper Code : Core - 4.1 <br> B.A. / B.Sc. $4^{\text {th }}$ Semester (Honours) 

1. If $y=x^{3}+x^{2}-1$, calculate the values of $y$ for $x=0,1,2,3,4$ and construct the difference table.
2. Construct a forward difference table from the following values $x$ and $y$

| $x$ | $:$ | 5 | 10 | 15 | 20 | 25 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $y$ | $:$ | 996 | 983 | 970 | 959 | 952 |

3. Construct a forward difference table, given that

| $x$ | $:$ | 5 | 10 | 15 | 20 | 25 | 30 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $y$ | $:$ | 9962 | 9848 | 9659 | 9397 | 9063 | 8660 |

4. Construct a forward difference table and find the $5^{\text {th }}$ term of the series :
$3,6,11,18$
5. Construct a forward difference table and find the $6^{\text {th }} \& 7^{\text {th }}$ terms of the series :
$0,4,16,42,88$
6. Construct a backward difference table from the following values $x$ and $y$

| $x$ | $:$ | 15 | 20 | 25 | 30 | 35 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $y$ | $:$ | 4025 | 5023 | 6018 | 7005 | 7089 |

7. Construct a backward difference table with the following data :

$$
u_{0}=30, \quad u_{1}=140, \quad u_{2}=870, \quad u_{3}=2230, \quad u_{4}=5290
$$

8. Evaluate the following problems ( $h$ being the interval of differencing ) :
(a) $\Delta \tan ^{-1} a x$
(b) $\Delta \sin 3 x \cos x$
(c) $\Delta \operatorname{coshax}$
(d) $\Delta \cot a^{x}$
9. Evaluate the following problems ( $h$ being the interval of differencing and $h=1$ ) :
(a) $\Delta^{2}\left(a b^{x}\right)$
(b) $\Delta^{3}[(1-x)(1-2 x)(1-3 x)]$
(c) $\Delta^{9}\left[\left(1-a x^{2}\right)\left(1-b x^{3}\right)\left(1-c x^{4}\right)\right]$
10. Prove that
$e^{x}=\left(\frac{\Delta^{2}}{E}\right) e^{x} \cdot \frac{E e^{x}}{\Delta^{2} e^{x}}$
the interval of differencing being unity (i.e., put $h=1$ )
